Synthesis method of high speed finite state machines

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Abstract. The paper is concerned with the problem of state assignment and logic optimization of high speed finite state machines. The method is designed for PAL-based CPLDs implementations. Determining the number of logic levels of the transition function before the state encoding process, and keeping the constraints during the process is the main problem at hand. A number of coding bits, as well as codes for the states, are adjusted to achieve a machine with a determined number of logic levels. Elements of two-level minimization are taken into consideration in the state assignment. The proposed optimization method is based on utilizing tri-state buffers, thus enabling achievement of a one-logic-level output block.

Key words: state assignment, Finite State Machines (FSM), Programmable Array Logic (PAL), Complex Programmable Logic Devices (CPLD), logic optimization, tri-state buffer.

1. Introduction

Two most popular families of programmable logic devices are FPGAs (Field Programmable Gate Arrays) and CPLDs (Complex Programmable Logic Devices). FPGAs are developed definitely faster than CPLDs, however, the structure of CPLDs is more efficient than LUT-based structures of the FPGAs [1–3].

A large majority of CPLDs are built of a simple cell matrix and a programmable interconnect array (PIA) – see Fig. 1.

![Typical CPLD structure](image)

Fig. 1. Typical CPLD structure

The core of most CPLDs is PAL-based cell. The generalized structure of the PAL-based cell is shown in Fig. 2.

![Generalized structure of PAL-based cell](image)

Fig. 2. Generalized structure of PAL-based cell

PAL-based cell contains a programmable-AND/fixed-OR structure (1), which can implement logic up to \( k \) product terms. In most cases \( k = 5 \) (Altera: MAX3000A; Xilinx: XC9500, MAX7000; Lattice: ispXPLD5000; Atmel: ATF1500). The output of an AND-gate cannot be connected to more than one OR-gate.

The register (in some cases programmable as D or T flip-flop) can be bypassed for combinational operation (2). An intrinsic part of the cell is the tri-state buffer (3). Generally, an OE input can be driven by a combinational circuit (usually an AND-gate) or is connected to logic 'high' or 'low'. The built-in tri-state buffer enables the expansion process, among other things.

Logic blocks contained in CPLD structures usually feature additional logic resources that can facilitate product term expansion. These resources include parallel expanders, folded NAND feedback lines, often referred to as shared expanders, logic allocators. The expanders enable unequal distribution of product terms between cells, and extending the number of products available for one function beyond the limit of \( k \) terms contained in one PAL block. Anyway they can only move the limit to a greater value, and they do not provide feasibility of implementation for every function. Additional expansion of the number of terms is thus necessary.

The proposed logic synthesis process consists of two main procedures:

- PAL-oriented state assignment,
- PAL-oriented two-level optimization of output block.

An overview of the logic synthesis system is shown in Fig. 3.

The state assignment is basic and the most important stage of FSMs synthesis. Despite the fact that methods considered as optimal were developed [4, 5], the works on the synthesis for CPLDs are still continued [6, 7]. To be certain, there are also many aims for the optimization, like reducing the
2. Theoretical background

2.1. The automata theory. The mathematical model of a sequential circuit is a Finite State Machine (FSM), which is a five-tuple: \( \{X, Y, S, \delta, \lambda\} \), where: \( X \) is a finite input alphabet, \( Y \) is a finite output alphabet, \( S \) is a finite set of states, \( \delta \) is the transition function, and \( \lambda \) is the output function. The transition function of an FSM determines the next state of the machine – the number of occurrences as a next state and primary outputs in the state graph, with a corresponding STT, is presented in Fig. 5.

Internal states of an FSM are given mostly symbolic values. The goal of the state assignment is to assign to every state a binary representation. The minimum number of code bits assigned to states, next states, and primary outputs (the kiss format). The rows of a STT are called symbolic implicants. A state transition graph, with a corresponding STT, is presented in Fig. 5.

2.2. Basic definitions. A multi-output implicant of a function \( f : B^n \rightarrow B^m \) is a pair of row vectors of dimension \( n \) and \( m \) called an input and an output part, respectively. The input vector items are taken from the set \( \{0, 1, \} \) and represents a product of literals. The output part has entries in the set \( \{0, 1, \} \). For each output component, a 1 implies a true or don’t care value of the function in correspondence with an input part. A multi-output Boolean function \( f : B^n \rightarrow B^m \) may be represented as a collection of \( m \) single-output functions \( f_i : B^n \rightarrow B^1 (i = 0, \ldots, m-1) \).

An assigned STT is a collection of multi-output implicants. An input part of a multi-output implicant corresponds to the primary input and a present state; whereas an output part of the same corresponds to a next state and the primary output. Generally, the \( \delta \) and \( \lambda \) functions are multi-output functions, so let \( \delta_i \) be \( i^{th} \) bit of the transition function and \( \lambda_j \) be \( j^{th} \) bit of the output function.

Let the state weight \( \eta^\delta_i \) be a number of transis to the state \( S_i \) of the machine – the number of occurrences as a next state in an STT.

Let \( \Delta_{f_i} \) be a number of implicants of the function \( f_i \), e.g. \( \Delta_{\delta_i} \) is the number of implicants of a simple transition function \( \delta_i \).

Let the \( \mu\)-range be the number of bits equal to 1 in the code.

The distance \( \nu(A, B) \) between two minterms \( A \) and \( B \) is the number of bits, they differ in. Let the \( \nu(S_i, S_j) \) be a number of code bits assigned to states \( S_i \) and \( S_j \) in which they differ in.

Let the \( \xi \) be the number of logic levels of the transition block.

Let \( card(Y) \) be the cardinality of the \( Y \) set.

In order to simplify and increase a clarity of figures, symbols of the PAL-based cell will be used in the paper, instead of drawing a full cell. The PAL-based cell symbols used in the paper are presented in Fig. 6.

Let \( \sigma_f \) be a number of PAL-based cells of the implementation of the function \( f \).
Let $\xi_f$ be a number of cascaded PAL-based cells in the longest signal path from the inputs to the outputs.

Product term expansion using feedbacks to a PIA causes an addition of extra logic levels to the structure. Let the structure of PAL-based cell (like in Fig. 6) insert to the path a delay defined as a one-logic-level. Hereafter in this paper, we will interpret the term “one-logic-level”, “$\xi_f$-logic-level” as the number of cascaded PAL-based cells in the longest signal path from the inputs to the outputs in the concerned circuit. The exception to this rule will be the terms “two-level minimization”, and “two-level optimization”. These terms are well established in the literature, and we will be used in their traditional meaning, i.e. “two-level” = two levels of logic gates.

2.3. Introduction to a state assignment. Because a coded STT is a collection of multi-output implicants, to decrease the number of implicants:

1. Codes should be minimal with respect to $\mu$-range.
2. States $S_i$ with greater weights $\eta^{S_i}$ should be assigned first.

The second conclusion is easy to explain – states that occur more frequently as next state are assigned codes with a smaller number of logic ‘high’. Before going ahead, one more thing should be noticed: the state with the greatest weight should be assigned the code with all ($\mu = 0$) bits logic low. This is because none of the single transition functions includes implicants corresponding to transition to the state. Elements that refer to the weights of states have been proposed in [12].

Considering the FSM realization, dedicated for PAL-based CPLDs, the number of implicants of every single function should fit the number of product terms best. So, the number of implicants should be known in the process of state assignment. Of course the number of terms may be reduced as the effect of two-level minimization. The main goal of the state assignment process should be to assign states with codes conveniently situated for implicant merger. It is complicated for FSMs, because the input parts of the multi-output implicants are connected with the output part. The next state of the transition is the present state of another transition. Changing one bit of the state code involves changes in both input and output part of the implicants. On the other hand, elements of two-level minimization must be included in the state assignment process, in order to take advantage of the number of the PAL-based cell terms. Primary and secondary merging conditions enable the algorithm to include elements of two-level minimization into the process of the state assignment.

2.4. Primary merging conditions. The idea of the state assignment is based on assigning to two states $S_p$ and $S_r$, which correspond to the transitions to another state $S_i$ for the same input $X$, binary codes that differ only in one position, $\nu(S_i, S_j) = 1$.

A fragment of an example FSM with two different state assignment is shown in Fig. 7. There are two transitions presented in the figure. The state $s3$ is the next state for both transitions. The inputs and the outputs are also the same for both transitions. The present states are $s1$ in first transition and $s2$ in the second transition. The state $s2$ should be assigned the code, such as the distance to the state $s1$ code is one ($\nu(s1, s2) = 1$). Two presented multi-output implicants can be merged into one implicant (right branch in figure). The distance for the case on the left branch in the figure is $\nu(s1, s2) = 2$. Implicants cannot be merged.

2.5. Secondary merging conditions. Product terms of the PAL-based cell cannot be shared among the functions. So the structure extorts independent realization of every function $f_i : \mathbb{B}^n \rightarrow \mathbb{B}$ for $i = 0, \ldots, m - 1$. The two-level minimization is carried out for every function $f_i$ independently (each function is minimized one at a time as a single-output function). As a result of the state assignment, the transition function $\delta_i$ can contain implicants, the distance of which is 1, but not as the effect of satisfying primary merging conditions. This can happen, if the transition function contains implicants that refer to:
transitions from two different actual states \( S_i \) and \( S_j \), that are carried out for the same input \( x_u \), if the distance between the codes of those states equals one – \( \nu(S_i, S_j) = 1 \).

- transitions from the same state \( S_i \) for two different inputs \( X_u \) and \( X_w \), the distance between which is also one – \( \nu(X_u, X_w) = 1 \).

Consider the example shown in Fig. 9. No primary merging conditions exist for the presented fragment of the unassigned STT. The states are assigned codes and then the list of multi-output implicants is split to single-output implicants (because product terms of PAL-based cell cannot be shared among the functions). The list of implicants is reduced to two after the two-level minimization. One pair of implicants is merged because there is pair of transitions from the states \( s1 \) and \( s3 \) for the same input \( 01 \) and the output has a 1 on the same position \( \delta_2 \). It is of course possible because the distance between codes of the states \( s1 \) and \( s3 \) equals one.

The second pair of implicants can be merged because there are transitions from the state \( s3 \) for two different inputs \( 01 \) and \( 11 \), the distance between which is one (\( \nu(X_u, X_w) = 1 \)) and two implicants that correspond to the transitions belong to the same function \( \delta_1 \).

**Definition 2.** A Secondary Merging Condition (SMC) \( \{S_p, S_r, S_a, S_b\}_{\delta, X} \) is a condition that is formed by two present states \( S_p \) and \( S_r \), from which there are transitions to next states \( S_a \) and \( S_b \) for the same input \( X \). The symbolic implicants, referring to the present states \( S_p \) and \( S_r \), belong to the same transition function \( \delta_1 \).

To satisfy the secondary merging conditions \( \{S_p, S_r, S_a, S_b\}_{\delta, X} \), the states \( S_p \) and \( S_r \) have to be assigned binary codes with the distance between them equal to one – \( \nu(S_p, S_r) = 1 \).

One more secondary merging condition \( \{S_p\}_{\delta, X_u, X_w} \) can be defined as a condition that is formed by the present state \( S_p \), from which there are transitions to the next states \( S_a \) and \( S_b \) for inputs \( X_u \) and \( X_w \). The symbolic implicants, referring to the present state \( S_p \), belong to the same transition function \( \delta_1 \). The secondary merging condition \( \{S_p\}_{\delta, X_u, X_w} \) is always fulfilled, and two implicants are merged. The condition is written in order to eliminate multiple merging of the same implicants.

SMCs emerge during the process of state assignment. One step of the state encoding process is shown in Fig. 10. The mechanism of the SMC arising is also presented.

**Definition 3.** The Implicants Distribution Table (IDT) \( T \) is a table divided into columns, corresponding to the weights \( \Delta_{\delta_1} \) of the single functions \( \delta_1 \). Every row of the table corresponds to the number of implicants which is equal to the weights of the states. These are written into those columns \( \Delta_{\delta_1} \), for which there is a 1 on \( i^{th} \) position of the code.

When the PMC or SMC is fulfilled, a \( -1 \) is written into the column corresponding to the function \( \delta_1 \), for which two implicants are merged.

### 2.7. Elements of two-level optimization.

Classical logic synthesis of combinational circuits implemented in great majority of vendor tools consists of two steps. First a two-level minimization is applied separately to every single-output function. Then, implementation of the minimized functions in PAL-based blocks, containing a predefined number of product terms, is performed. If the number of implicants \( \Delta_{f, \delta_1} \), representing a function after minimization, is greater than the number of product terms \( k \), available in a logic block, a greater number of logic blocks has to be utilized to implement the function. The classical product term expansion method consists in utilizing feedback lines to build a multi-level cascaded structure, which increases propagation delays significantly.

![Fig. 11. The example of product term expansion exploiting tri-state output buffers](image)
Consider the function \( y = ac\overline{d} + ab\overline{c}d + bc\overline{e} + \overline{a}cd + \overline{a}d \). This function can be implemented using two PAL-based logic blocks with 3 terms per output and tri-state output buffers (Fig. 11).

Product term expansion that exploits tri-state output buffers seems to be the most attractive solution, as it does not lead to expansion of logic levels. This idea is the basis of two-level optimization.

3. The design method

3.1. PAL-oriented state assignment. The main cost of expanding product terms using feedbacks to a PIA is a reduction of the system speed, caused by the added extra logic levels to the structure. The number of logic levels of fast automata must be as few as possible. The logic level extraction problem is solved in the presented approach.

If the number of logic levels of the transition function \( \xi \) were known before the state assignment, the number of code bits and codes as such could be adjusted to achieve the number of logic levels. The question is: is it possible to estimate the minimum number of logic levels of the transition block, for which a realization is possible? The answer is yes. It can be determined from the Eq. (2).

\[
\xi = \begin{cases} 
1 & \text{if } \eta_S < k \\
\lfloor \log_2 \eta_S \rfloor & \text{if } \eta_S \geq k 
\end{cases} \tag{2}
\]

where \( \eta_S \) is the greatest but one weight (unless there are two, or more states with the same greatest weight). Why the greatest, but only one? Because the state with the greatest weight is assigned the zero code, so none of the functions has implicants corresponding to transitions to the state. Of course the logic level number of the transition block \( \xi \) is equal to the number of cells used in the longest path.

The main idea is to count the number of logic levels of a block for every single transition function during the state assignment process. In the following steps of the algorithm, unassigned state with the greatest weight, is assigned a minimum \( \mu \)-range code. If the number of logic levels exceeds the assumption, the number of coding bits is increased. Codes already assigned to states are supplemented with 0.

The algorithm 1 (state assignment oriented on the minimization of logic levels):

1. Calculate the number \( K \) of bits of coding word (Eq. (1)).
2. Specify the PMCs of the transition function.
3. Assign to the state with the greatest weight \( \eta^* \) the zero code \( (\mu = 0) \). If there is more than one state that satisfies the condition, choose the state \( s_i \) which can satisfy most PMCs \( \{s_i, s_r\}_x \).
4. \( \mu := 1 \).
5. Calculate the number \( \xi \) of logic levels of the transition function (Eq. (2)).
6. Choose the state with the greatest weight \( \eta^+ \). If there is more than one state that satisfies the condition, the sort key is as follows:

- (a) choose the state \( s_i \), which can satisfy more primary merging conditions \( \{s_i, s_r\}_x \).
- (b) choose the state \( s_i \), which can satisfy more non-excluding secondary merging conditions \( \{s_i, s_r\}_x \).
7. If none of the \( \mu \)-range codes is free, \( \mu := \mu + 1 \).
8. Assign to the chosen state \( s_i \) a free code of the \( \mu \)-order; if there is more than one possibility, the sort key is as follows:

- (a) the number of PAL-based cell incrementation is the smallest,
- (b) the sum of all \( \Delta_{k} \), is the smallest,
- (a) and (b) are calculated after making allowance for every satisfied merging condition)
9. If exists \( \delta_i : \xi_i > \xi_i \), then:

- (a) cancel the last assignment,
- (b) \( K := K + 1 \),
- (c) \( \mu := 1 \),
- (d) supplement the already assigned codes with 0 on the MSB,
- (e) return to point 8.
10. Refresh the IDT.
11. Revise the secondary merging conditions.
12. Cancel the satisfied or the excluded primary and secondary merging conditions.
13. If not all states have been already encoded, than return to point 6.
14. End.

Let’s consider an example. The STT of the example FSM with weights of states are given in Fig. 12 (kiss2). The coding length \( K \) is 4. It has been assumed that \( k = 5 \). The number of logic levels is determined on the basis of weight of the state 4 and of course equals one.
Next, states 6, 7, 13 and 4 are assigned respectively 0001, 0010, 0100 and 1000. According to the definition 3, the weights of states are written into those columns $\delta_i$, for which there is a 1 on the $i^{th}$ position of the code. Four rows of the presented in Fig. 13 part of the IDT correspond to the numbers of implicants, which are equal to weights of the states, that is 2.

Because none of the 1-range codes are free, so $\mu := 2$. First, the state 8 is assigned 0011, and then the state 11 is assigned 1010. The SMC $\{7,11\}$ of the column corresponding to the function $\delta_1$ ($\Delta_1$ is decremented). A similar situation occurs after encoding the state 9. Next, states 2, 10, 12 and 14 are encoded.

First, the state 8 is assigned 0011, and then the state 11 is assigned 1010. The SMC $\{7,11\}$ is fulfilled, so a $-1$ is written into ITD for the column corresponding to the function $\delta_1$ ($\Delta_1$ is decremented). A similar situation occurs after encoding the state 9. Next, states 2, 10, 12 and 14 are encoded.

A starting point to assign state 5 is an IDT form Fig. 13. The state 5 should be assigned one of the free code, e.g. 1011. Using this code, as well as any other free code, makes the structure of the transition function two-logic-level. In this situation, an additional bit of code must be used. A state 5 is assigned with code 10000. The number of the logic levels still remains one, and used logic cells are smaller than in the case of using 4-bit codes. Codes, which are already used, are supplemented with 0 on the MSB position. An assignment of the state 5 is presented in Fig. 14.

### 3.2. PAL-oriented two-level optimization

The concept of two-level optimization of FSM's output block lies in the background of the original method of product term expansion utilizing tri-state terminals.

The set of multi-output implicants of a Boolean output function $f : \mathbb{B}^n \rightarrow \{0, 1, \ldots, m\}$ serves as the starting point for a two-level optimization. The two-level optimization consists of a two-level splitting minimization, PAL-oriented term partitioning, and PAL mapping. The optimization process starts with the two-level splitting minimization. Then partitioning of the individual minimized functions is performed. As a result of the two procedures, the set of implicants of a Boolean function is divided into subsets with cardinality less than the number of terms available in one PAL-based cell.

The objective of the classical two-level minimization is to reduce both the number of products in the Boolean formula representing a function, and the number of literals in a product. Because of a limited number of multi-input terms available in PAL-based cell, the primary goal of the two-level splitting minimization is to reduce the number of products. Reduction of literals is non-essential. The idea of the two-level splitting minimization is presented in Fig. 15.

Fig. 13. State assignment process

![Fig. 13. State assignment process](image)

Fig. 14. Example function with IDTs being the effects of the different state assignment

![Fig. 14. Example function with IDTs being the effects of the different state assignment](image)

The process of two-level splitting minimization starts from classical two-level minimization using the Espresso algorithm. Then, modification of individual minimized functions is executed in succession by means of an implicant splitting procedure.

Let an implicant $A_{ys} = a_{(n-1)s}, \ldots, a_{1s}, a_{0s}$ covers $2^s$ minterms of single-output function $y = \sum \left(i_{(n-1)s}, \ldots, i_1, i_0\right)$ that form the set of minterms $I_s$, whereas implicant $A_{xt} = a_{(n-1)t}, \ldots, a_{1t}, a_{0t}$ covers $2^t$ minterms that form the
Modification, that would not change the set of minterms.

The consecutive steps of splitting implicators for one function of \(5xp/1\) are presented in Fig. 16.

After two-level splitting minimization, PAL-oriented term partitioning is executed. The objective of the PAL-oriented term partitioning procedure is to subdivide the set of implicators into subsets, for which cardinality is less or equal to the number of terms \((k)\) available in PAL-based cell.

Let us consider the function from Fig. 15. Let us assume that the function is to be realized by means of the PAL-based logic cells, each of them containing 3 terms. Having completed the two-level splitting minimization, we obtained the result shown in the left-hand column of Table 1. Then we attempt to find the partition of \(y\) function implicators into such two subsets \(Y_1\) and \(Y_2\), that cardinality of the \(Y_1\) set is less or equal to the number of terms \((k)\) included in PAL-based logic cells \((\text{card}(Y_1) \leq k)\), while \((\text{card}(Y_2) = \text{min})\). The theoretical background of PAL-based partitioning is presented in [13].

In the example \(i4\) implied partition of implicators into two subsets \(Y_1\) and \(Y_2\), for which \(\text{card}(Y_1) = 3\) and \(\text{card}(Y_2) = 4\) is presented in the next column of Table 1. The first one characterizes the \(y_1\) function that is active for \(i4 = 0\) (Table 1, column 2), while the second one is related to the function \(y_2\) being active for the vectors \(i4 = 1\) (Table 1, column 3).

In the next step, the partitioning of \(y_2\) function implicators is executed. A variable \(i2\) implied partition of implicators into two subsets \(Y_{21}\) (function \(y_{21}\)) and \(Y_{22}\) (function \(y_{22}\)), for which \(\text{card}(Y_{21}) = \text{card}(Y_{22}) = 2 < k\), presented in the 4th and 5th column of Table 1 respectively.

### Table 1

<table>
<thead>
<tr>
<th>(y.pla)</th>
<th>(y_1) active, if (i4 = 0)</th>
<th>(y_2) active, if (i4 = 1)</th>
<th>(y_{21}) active, if (i4/2 = 10)</th>
<th>(y_{22}) active, if (i4/2 = 11)</th>
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<tbody>
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<td>.ib i4,i3,i2,i1,i0</td>
<td>.ib i4,i3,i2,i1,i0</td>
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<td>00000 1</td>
<td>1 0 1</td>
<td>1 0 1</td>
<td>111 1</td>
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<td>10101 1</td>
<td>10010 1</td>
<td>10010 1</td>
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### Fig. 16. Consecutive steps of splitting procedure (only input part of implicators)
The PAL-oriented partitioning scheme and PAL mapping of the $y$ function using blocks consisting of three terms are presented in Fig. 17.

![Fig. 17. Results of PAL-oriented partitioning and PAL mapping](image)

The two-level optimization is especially attractive with respect to dynamic parameters. The algorithms discussed above can be used as independent FSM synthesis methods, improving the dynamic properties of final solutions.

An implementation of the $ex4$ automaton after state assignment and optimization is presented in Fig. 18.

![Fig. 18. Implementation of the $ex4$ automaton](image)

4. Experimental results

The experiments were carried out by means of:

- JEDI [14]: the input dominant algorithm (i), the output dominant algorithm (o) and the coupled dominant algorithm (c);
- NOVA [4]: the input and output (dominance) constraints (iohybrid code – io), the input constraints (hybrid code – ih) and the input constraints (exact code – ie);
- the presented ml-algorithm (ml) and two-level optimization (ml+o).

Experiments were carried out using some selected benchmarks [15].

4.1. Analysis. Experimental results are presented in form of graphs. Two conceptions of graphs were applied:

- yield of the logic cells $U_{\sigma f}$ and yield of the logic levels $U_{\xi f}$,
- direct comparison of selected benchmarks.

The yield of the logic cells $U_{\sigma f}$ is calculated from the equation:

$$U_{\sigma f} = \frac{(\sum_{\sigma f})_A - (\sum_{\sigma f})_M}{(\sum_{\sigma f})_A} \times 100\%,$$

where $(\sum_{\sigma f})_A$ denotes the average of cells of implementation for the function $f$ for all the benchmarks, while the average is calculated for all tested methods; $(\sum_{\sigma f})_M$ denotes the whole number of cells of the selected benchmarks for selected encoding methods. The yield of the logic levels $U_{\xi f}$ is calculated analogically to the yield of the logic cells $U_{\sigma f}$.

The yield of the logic cells (levels) should be interpreted as a percent of the number of the logic cells (levels) for which selected method is better (or worst if the yield is negative) than the average. The yield is calculated for 36 benchmarks (bbara, bbsse, bbtas, beecount, cse, dk14, dk15, dk16, dk17, dk27, dk512, ex1, ex4, ex6, keyb, lion, lion9, mark1, mc, opus, pma, s1, s208, s27, s386, s420, s820, s832, sand, sse, sty, tav, tbk, tma, train11, train4).

![Fig. 19. Yield of the logic cells $U_{\sigma f}^{\delta+\lambda}$ and logic levels $U_{\xi f}^{\delta+\lambda}$ for different methods](image)
be additionally improved as an effect of two-level optimization of the output block. The yield $U^{\xi+\lambda}$ for ml+o method exceeds 20%. Of course, in many cases reduction of the logic levels is relevant with utilization of the excessive PAL-based cells. For the whole group of benchmarks the yield of logic cells $U^{\sigma+\lambda}$ is about -10% for ml algorithm and nearly 15% for ml+o method.

Direct comparison of selected benchmarks (bbsse, ex4, keyb, s420, sand) is presented in Fig. 20 and Fig. 21 for the transition and output block respectively.

Fig. 20. Direct comparison of selected benchmarks: a transition block

Fig. 21. Direct comparison of selected benchmarks: an output block

The logic levels $\xi$ obtained after state encoding by ml algorithm are the same (bbsse, ex4, s420, sand) or better (keyb) than results obtained by NOVA or JEDI. Moreover the results obtained for keyb benchmark are the best in respect to logic cells $\sigma$ in comparison to NOVA nad JEDI. However, in some cases ml algorithm carries out to utilize more logic cells than NOVA or JEDI (s420). In other cases results are comparable.

Analyzing the results of logic levels $\lambda$ of the output block is always one-logic-level (for the whole set of 36 analyzed benchmarks). Sometimes there should be used extra logic cells to achieve one-logic-level output block as the effect of two-level optimization (ml+o) like for s420 or sand benchmarks.

4.2. Interface to vendor tools. If thousands of experiments are to be carried out, interfacing prototype software to tools supplied by PLD vendors becomes an important issue. Software tools developed by companies or institutions independent from PLD vendors are capable of performing only the logic synthesis stage. Then, the design has to be transferred to a vendor-specific system for completing the implementation stage. This regards also academic software, developed by research teams.

The main problem in porting a design to a vendor-specific system is to find an appropriate intermediate format for the design data exchange. Commercial vendor-independent systems (e.g. Synplify, Leonardo Spectrum, Precision RTL) use low level netlists for this purpose. This approach is secure, because there is little chance, that the low level structure will be interfered with by implementation tools. The method is however not universal, because low level netlists contain much vendor-specific and architecture-specific information. Using this approach thus requires equipping the synthesis software with procedures or plugins responsible for converting formats, and preparing data specifically for the implementation tools. This is acceptable for commercial companies, but difficult for academic research teams, as it requires much “scientifically worthless” extra work.

It was thus desirable to find alternative formats for the data exchange, possibly more universal, and using a higher level of abstraction. Here using a Hardware Description Language (HDL) seems to be the most obvious, and natural choice. Choosing the right abstraction level for the intermediate format is an important task, because vendor implementation software can change and “destroy” logical structures generated by synthesis tools.

Behavioral HDL description seems to be the design specification format most preferred for design entry nowadays. Because of its high abstraction level it allows the designer to concentrate on proper description of the desired functionality. As a textual format, following the standard of the chosen language, it is universal and portable between technologies and software tools.

A number of experiments were carried out to examine various synthesis tools, and, in particular, the effects of selecting different data exchange formats, on the quality of results. The tools were tested using the standard benchmarks [15]. The test circuits were implemented in CPLD structures.

It turned out that, if behavioural description was used as the entry format, the quality of the solutions was not good. High abstraction level in behavioural modeling gives a large degree of freedom to the software. Logical structures can eas-
ily be “spoiled” by vendor implementation programs. During the experiments it turned out, that it is possible to propose as the intermediate format a style of VHDL description, lying at a lower level of abstraction, than behavioural modeling, but still portable between software tools, and comprehensible to a human. The proposed style of VHDL modeling resembles the dataflow description commonly known in the literature. More details are reported in [13, 16].

5. Conclusions

The paper concerns the problem of high speed finite state machine designing. The automata are to be implemented in PAL-based structure, which is the core of most CPLDs.

An original method of state assignment and optimization is developed. The non-minimal state encoding is based on determining the number of the logic levels of the transition function and adjusting the number of coding bits to keep the constraints. The second idea is to keep the output block one-logic-level thanks to utilizing tri-state buffers.

REFERENCES